



## DETAILED SOLUTIONS AND CONCEPTS - INTRODUCTION TO EXPONENTS AND ROOTS

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Thank you!

**PLEASE NOTE THAT YOU CANNOT USE A CALCULATOR ON THE ACCUPLACER  
- ARITHMETIC TEST! YOU MUST BE ABLE TO DO THE FOLLOWING PROBLEMS  
WITHOUT A CALCULATOR!**

### Exponents

Exponents or powers indicate how many times a number is multiplied by itself.

Following are some examples:

- $3^0$  indicates **1**. The value of any number with an exponent of  $0$  equals  $1$ . The only exception is  $0$ . When raising it to the  $0$  power, its value is *undefined*.
- $3^1$  indicates **3**. It is customary in mathematics NOT to write the exponent  $1$ .
- $3^2$  indicates  **$3(3) = 9$** .

NOTE: Numbers that result from other numbers being raised to a power are also referred to as **perfect powers**!

$3^2$  is called an **exponential expression** and is read as "3 squared" or "three to the second power" or "three raised to the second power."

$3$  is called the **base** and  $2$  is called the **exponent** or **power**. The power indicates how many times the base is supposed to be multiplied by itself.

- $3^3$  indicates  **$3(3)(3) = 27$** . It is read as "three cubed" or "three to the third power" or "three raised to the third power."
- $3^4$  indicates  **$3(3)(3)(4) = 81$** . It is read as "three to the fourth power" or "three raised to the fourth power."

## Roots

Finding a root reverses the operation of finding a power. The **radical sign**  $\sqrt{\quad}$  indicates this process.

Following are some examples!

- To undo  $3^4 = 81$ , we write  $\sqrt[4]{81} = 3$ , where **4** is called the **index** and **81** is called the **radicand**. It is read as the "fourth root of 81." We call  $\sqrt[4]{81}$  a **radical expression**.
- To undo  $3^3 = 27$ , we write  $\sqrt[3]{27} = 3$ . It is read as the "third root of 27" or the "cube root of 27."
- To undo  $3^2 = 9$ , we write  $\sqrt{9} = 3$ . It is read strictly as the "square root of 9." **Please note when the index is 2 it is customarily left off.**

What about  $\sqrt{10}$ . Here we don't immediately know a number that when multiplied by itself results in a product of 10. Usually, these radicals are evaluated using a calculator. If a calculator is not handy, we can make a rough estimate and say that the value of  $\sqrt{10}$  must be slightly greater than 3 because we know that  $\sqrt{9} = 3$ .

### Problem 1:

Evaluate  $10^3$ .

$$10(10)(10) = 1,000$$

### Problem 2:

Evaluate  $2^5$ .

$$2(2)(2)(2)(2) = 32$$

### Problem 3:

Evaluate  $3.4^2$ .

$$3.4(3.4) = 11.56$$

### Problem 4:

Evaluate  $5,982^0$ .

The value of any number with an exponent of  $0$  equals  $1$ .

$$5,982^0 = 1$$

### Problem 5:

Evaluate  $1^{23}$ .

Since  $1(1)(1)(1)(1) \dots (1)$  always equals 1 no matter how many times we multiply it by itself, we can say that

$$1^{23} = 1$$

### Problem 6:

Evaluate  $0^{41}$ .

Since  $0(0)(0)(0)(0) \dots (0)$  always equals 0 no matter how many times we multiply it by itself, we can say that

$$0^{41} = 0$$

### Problem 7:

Evaluate  $\sqrt{1}$ .

Since  $1(1) = 1$ , no matter what the index, a radical expression containing a radicand of  $1$  always has a value of  $1$ .

That is,  $\sqrt{1} = 1$ .

### Problem 8:

Evaluate  $\sqrt{0}$ .

Since  $0(0) = 0$ , no matter what the index, a radical expression containing a radicand of  $0$  always has a value of  $0$ .

That is,  $\sqrt{0} = 0$ .

### Problem 9:

Evaluate  $\sqrt{36}$ .

Since  $6(6) = 36$ , we can say that  $\sqrt{36} = 6$ .

**Problem 10:**

Evaluate  $\sqrt{100}$ .

Since  $10(10) = 100$ , we can say that  $\sqrt{100} = 10$ .

**Problem 11:**

Evaluate  $\sqrt{81}$ .

Since  $9(9) = 81$  we can say that  $\sqrt{81} = 9$ .

**Problem 12:**

Evaluate  $\sqrt{400}$ .

Since  $20(20) = 400$ , we can say that  $\sqrt{400} = 20$ .

**Problem 13.**

Evaluate  $\sqrt{0.64}$ .

We know that  $8(8) = 64$ . Then  $0.8(0.8) = 0.64$ . Therefore,  $\sqrt{0.64} = 0.8$

**Problem 14:**

Considering perfect squares, find two successive decimal numbers between which the value of  $\sqrt{0.69}$  is located.

**NOTE: Numbers that result from other numbers being raised to the second power are also referred to as "perfect squares"!**

We know that  $\sqrt{0.64} = 0.8$  and  $\sqrt{0.81} = 0.9$ .

Therefore, the value of  $\sqrt{0.69}$  must be between  $0.8$  and  $0.9$ .

**Problem 15:**

Considering perfect squares, find two successive decimal numbers between which the value of  $\sqrt{0.55}$  is located.

We know that  $\sqrt{0.49} = 0.7$  and  $\sqrt{0.64} = 0.8$ .

Therefore, the value of  $\sqrt{0.55}$  must be between  $0.7$  and  $0.8$ .